

# RELATIVISTIC AND NON RELATIVISTIC

Before moving to the practical lets see the basic terms and definition for proper understanding:

## **Relativistic Bosons:**

Relativistic bosons are particles that obey Bose-Einstein statistics and have energies comparable to their rest mass energy. The distribution function for bosons is given by the Bose-Einstein distribution:

$$n(E) = \frac{1}{\exp\left(\frac{E-\mu}{k_B T}\right) - 1}$$

where:

- $E$  is the energy of the particles.
- $\mu$  is the chemical potential.
- $k_B$  is the Boltzmann constant.
- $T$  is the temperature.

The density of states  $g(E)$  in three dimensions for relativistic particles (considering spin  $s$  and volume  $V$ ) is:

$$g(E) = \frac{2s \cdot 4\pi V}{h^3 c^3} E^2$$

The particle distribution with respect to energy is given by:

$$\frac{dN}{dE} = g(E) \cdot n(E)$$

## **Non-relativistic Bosons:**

Non-relativistic bosons are particles whose kinetic energy is much less than their rest mass energy. The distribution function for bosons is still the Bose-Einstein distribution, but the density of states  $g(E)$  for non-relativistic particles is different:

$$g(E) = \frac{(2s+1) \cdot 2\pi V (2m)^{3/2}}{h^3} E^{1/2}$$

Here,  $m$  is the mass of the particles. The particle distribution with respect to energy remains:

$$\frac{dN}{dE} = g(E) \cdot n(E)$$

## Relativistic Fermions:

Relativistic fermions are particles that obey Fermi-Dirac statistics and have energies comparable to their rest mass energy. The distribution function for fermions is given by the Fermi-Dirac distribution:

$$n(E) = \frac{1}{\exp\left(\frac{E-\mu}{k_B T}\right) + 1}$$

The density of states  $g(E)$  in three dimensions for relativistic particles is:

$$g(E) = \frac{2s \cdot 4\pi V}{h^3 c^3} E^2$$

The particle distribution with respect to energy is:

$$\frac{dN}{dE} = g(E) \cdot n(E)$$

## Non-Relativistic Fermions:

Non-relativistic fermions are particles whose kinetic energy is much less than their rest mass energy. The Fermi-Dirac distribution still applies. The density of states  $g(E)$  for non-relativistic particles is:

$$g(E) = \frac{(2s+1) \cdot 2\pi V (2m)^{3/2}}{h^3} E^{1/2}$$

The particle distribution with respect to energy is:

$$\frac{dN}{dE} = g(E) \cdot n(E)$$

## EXPERIMENT 8

**AIM:** Plot the distribution of particles w.r.t. energy ( $dN/dE$  versus  $E$ ) in 3 Dimensions for relativistic bosons both at high and low temperature.

### CODE:

```
clc;clf;clear;
e=1.6e-19;,Kb=1.38e-23;h=6.626e-34;s=1;u=-1;V=1;c=3e8; //initialising the constant
E=0:0.001:0.5 //in MeV
T=[10^8 10^9];
Cr=(2*s*4*3.14*V)/((h^3)*(c^3)); //defining g(E)
for j=1:length(T)
    b=1/(Kb*T(j));
    for i=1:length(E)
        g(i)=Cr*(E(i))^2;
        n(j,i)=1/(exp((E(i)-u)*10^6*e*b)-1);
```

```

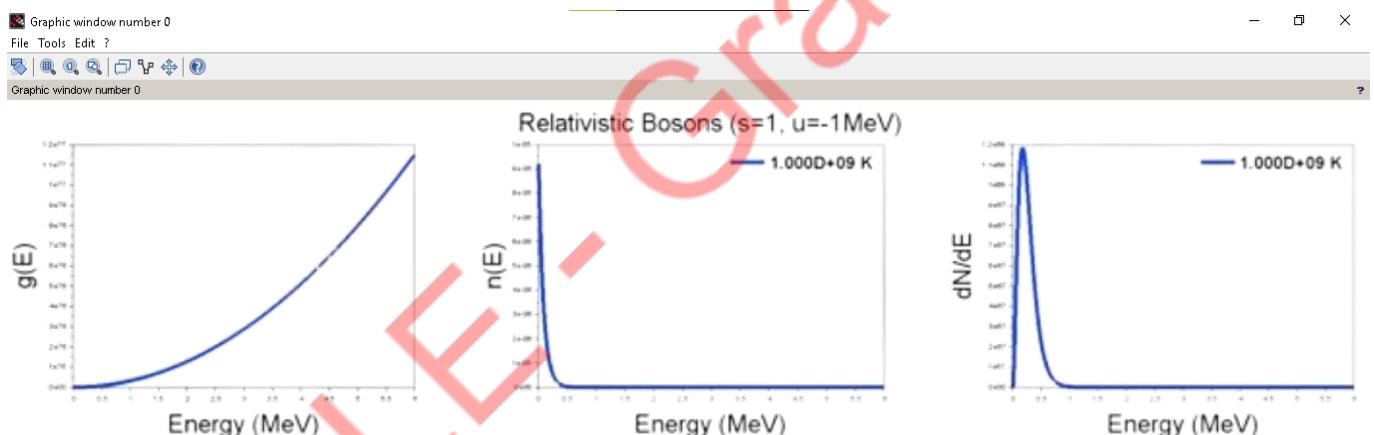
f(j,i)=g(i)*n(j,i); //defining dN/dE
end
subplot(2,3,j*j) //plotting the graphs
plot(E',g,'linewidth',4);
ylabel('g(E)', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4);

subplot(2,3,j*j+1)
plot(E',n(j,:)', 'linewidth',4); legend(string(T)+'K');
ylabel('n(E)', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4);
title('Relativistic Bosons(s='+string(s)+',u='+string(u)+'MeV)');

subplot(2,3,j*j+2)
plot(E',f(j,:)', 'linewidth',4); legend(string(T)+'K');
ylabel('dN/dE', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4)

```

end

**OUTPUT:****EXPERIMENT 9**

**AIM:** Plot the distribution of particles w.r.t. energy ( $dN/dE$  versus  $E$ ) in 3 Dimensions for non-relativistic bosons both at high and low temperature.

**CODE:**

```

clc;clf;clear;
e=1.6e-19;,Kb=1.38e-23;h=6.626e-34;s=1;u=-1;V=1;
m = 4*1.66e-27; //initialising the constant
E=0:0.001:0.5 //in eV
T=[100 1000];
Cn=((2*s+1)*(2*3.14*V)*(2*m)^1.5)/(h^3); //defining g(E)
for j=1:length(T)

```

```

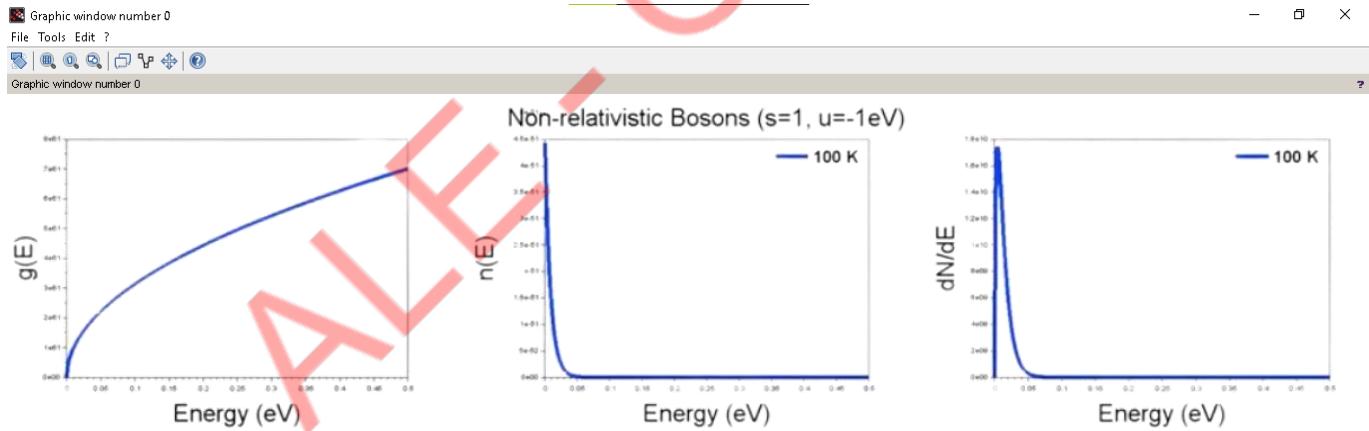
b=1/(Kb*T(j));
for i=1:length(E)
g(i)=Cn*(E(i))^2;
n(j,i)=1/(exp((E(i)-u)*e*b)-1);
f(j,i)=g(i)*n(j,i); //defining dN/dE
end
subplot(2,3,j*j) //plotting the graphs
plot(E',g, 'linewidth',4);
ylabel('g(E)', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4);

subplot(2,3,j*j+1)
plot(E',n(j,:)', 'linewidth',4); legend(string(T(j))+ 'K');
ylabel('n(E)', 'fontsize',4);
xlabel('Energy(eV)', 'fontsize',4);
title('Non Relativistic Bosons(s=' +string(s)+ ',u=' +string(u)+ 'eV)');

subplot(2,3,j*j+2)
plot(E',f(j,:)', 'linewidth',4); legend(string(T(j))+ 'K');
ylabel('dN/dE', 'fontsize',4);
xlabel('Energy(eV)', 'fontsize',4)
end

```

## OUTPUT:



## EXPERIMENT 10

**AIM:** Plot the distribution of particles w.r.t. energy ( $dN/dE$  versus  $E$ ) in 3 Dimensions for relativistic fermions both at high and low temperature.

## CODE:

```

clc;clf;clear;
e=1.6e-19;,Kb=1.38e-23;h=6.626e-34;s=0.5;u=1; //initialising the constants
V=1;c=3e8;

```

```

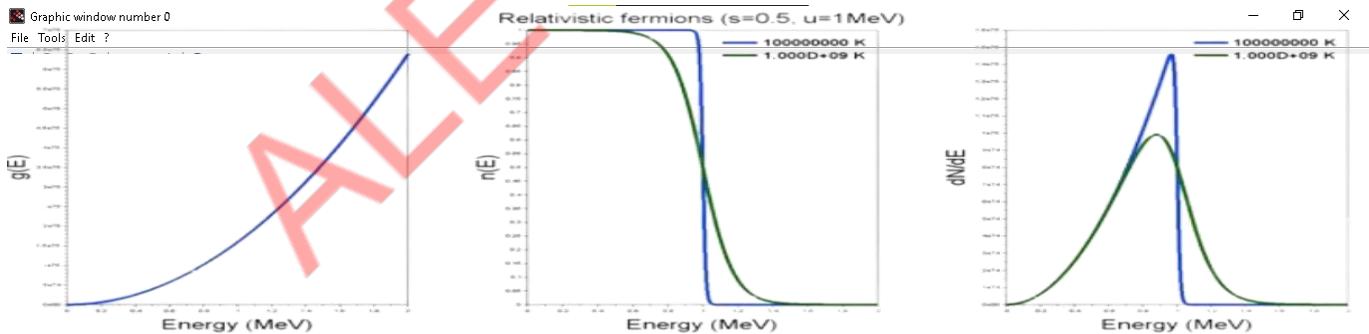
E=0:0.001:2 //in MeV
T=[10^8 10^9];
Cr=(2*s*4*3.14*V)/((h^3)*(c^3)); //defining g(E)
for j=1:length(T)
    b=1/(Kb*T(j));
    for i=1:length(E)
        g(i)=Cr*(E(i))^2;
        n(j,i)=1/(exp((E(i)-u)*10^6*e*b)+1);
        f(j,i)=g(i)*n(j,i); //defining dN/dE
    end
end
subplot(1,3,1) //plotting the graphs
plot(E',g,'linewidth',4);
ylabel('g(E)', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4);

subplot(1,3,2)
plot(E',n,'linewidth',4); legend(string(T)+' K');
ylabel('n(E)', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4);
title('Relativistic Fermions(s='+string(s)+',u='+string(u)+' MeV)');

subplot(1,3,3)
plot(E',f,'linewidth',4); legend(string(T)+' K');
ylabel('dN/dE', 'fontsize',4);
xlabel('Energy(MeV)', 'fontsize',4)

```

## OUTPUT:



## EXPERIMENT 11

**AIM:** Plot the distribution of particles w.r.t. energy ( $dN/dE$  versus  $E$ ) in 3 Dimensions for non-relativistic fermions both at high and low temperature.

## CODE:

```
clc;clf;clear;
```

```

e=1.6e-19; Kb=1.38e-23; h=6.626e-34; s=0.5; //initialising the constant
u=1; V=1; m=9.1e-31;
E=0:0.001:2 //in eV
T=[100 1000];
Cn=(2*s+1)*(2*3.14*V*(2*m)^1.5)/(h^3); //defining g(E)
for j=1:length(T)
    b=1/(Kb*T(j));
    for i=1:length(E)
        g(i)=Cn*(E(i))^0.5;
        n(j,i)=1/(exp((E(i)-u)*e*b)+1);
        f(j,i)=g(i)*n(j,i);
    end
end
subplot(1,3,1) //plotting the graphs
plot(E',g,'linewidth',4);
ylabel('g(E)', 'fontsize',4);
xlabel('Energy(eV)', 'fontsize',4);

subplot(1,3,2)
plot(E',n,'linewidth',4); legend(string(T) + 'K');
ylabel('n(E)', 'fontsize',4);
xlabel('Energy(eV)', 'fontsize',4);
title('Non-Relativistic Fermions(s=' + string(s) + ',u=' + string(u) + 'eV)');

subplot(1,3,3)
plot(E',f,'linewidth',4); legend(string(T) + 'K');
ylabel('dN/dE', 'fontsize',4);
xlabel('Energy(eV)', 'fontsize',4)

```

## OUTPUT:

