

Free Study Material from All Lab Experiments



**Thermodynamics Notes
for NET/GATE Physical Sciences
Born-Hyper & Other Topics #**

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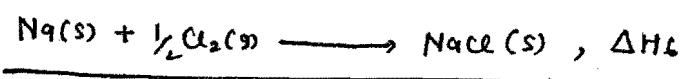
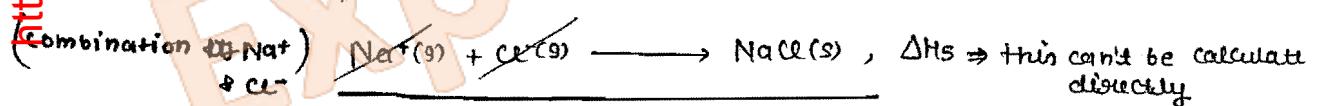
⇒ Born - Haber Cycle ⇒

Born-Haber cycle is used to calculate lattice energy. Lattice Energy can't be calculated experimentally but with the application of BH cycle we are able to calculate lattice energy.



"Lattice Energy is defined as the energy required to separate one mole of solid ionic compound into gaseous ion."

Formation of NaCl Crystall from $\text{Na}(\text{s}) + \text{Cl}_2(\text{g})$



[Practically Impossible]

from Hess's Law -

$$\Delta H_6 = \Delta H_1 + \Delta H_2 + \Delta H_3 + \Delta H_4 + \Delta H_5$$

By the appl' of Hess's law & Born-Haber's Cycle ⇒

We know, $\Delta H_1, \Delta H_2, \Delta H_3, \Delta H_4, \Delta H_6$
then,

$$\boxed{\Delta H_5 = \Delta H_6 - (\Delta H_1 + \Delta H_2 + \Delta H_3 + \Delta H_4)}$$

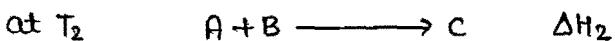
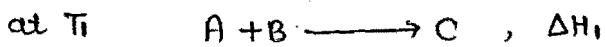
↓
(Lattice Energy)

$$\Rightarrow \Delta H_5^{\circ}(\text{NaCl}) = -410.87 \text{ kJ mol}^{-1}$$

\Leftrightarrow Kirchhoff's Equation : \Rightarrow

(Variation of temp., ΔH)

Ex) -Qn Rxn at ΔH doesn't \neq diff. temp.
By
Kirchhoff Eqⁿ



$$\Delta H = H_2 - H_1$$

$$\left(\frac{\partial (\Delta H)}{\partial T} \right)_P = \left(\frac{\partial (H_2)}{\partial T} \right)_P - \left(\frac{\partial (H_1)}{\partial T} \right)_P$$
$$= (C_P)_{P, \text{exp}} - (C_P)_{\text{Ref.}}$$

$$\left(\frac{\partial (\Delta H)}{\partial T} \right)_P = \Delta C_P$$

$$\partial (\Delta H) = \Delta C_P \cdot \partial T$$

Inte. both side

$$\int_{H_1}^{H_2} \partial (\Delta H) = \Delta C_P \int_{T_1}^{T_2} \partial T$$

$$\boxed{\Delta H_2 - \Delta H_1 = \Delta C_P (T_2 - T_1)}$$

Variation of heat of reaction with temp.

mathematical form of this statement is
Kirchhoff Eqⁿ

Kirchhoff Eqⁿ can be express either in terms of ΔH or ΔE

Kirchoff's Equation in term of ΔE .

$$\therefore \Delta E = E_2 - E_1$$

$$\left(\frac{\partial (\Delta E)}{\partial T} \right)_V = \left(\frac{\partial E_2}{\partial T} \right)_V - \left(\frac{\partial E_1}{\partial T} \right)_V$$

$$\left(\frac{\partial (\Delta E)}{\partial T} \right)_V = (C_V)_{P,T} - (C_V)_{R,T}$$

$$\left[\frac{\partial (\Delta E)}{\partial T} \right]_V = \Delta C_V$$

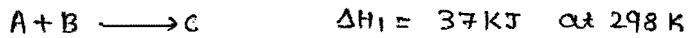
$$\partial (\Delta E) = \Delta C_V \cdot \partial T$$

Int on both side

$$\int_{\Delta E_1}^{\Delta E_2} \partial (\Delta E) = \Delta C_V \int_{T_1}^{T_2} \partial T$$

$$\boxed{\Delta E_2 - \Delta E_1 = \Delta C_V (T_2 - T_1)}$$

Numerical \Rightarrow



where C_p of (C \Rightarrow product) $\Rightarrow 5$

$$(C_p)_B = 3$$

$$(C_p)_A = 1$$

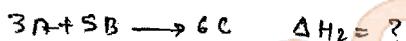
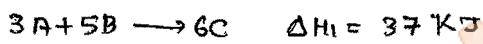
$$\Delta H_2 - 37 = \frac{1}{2} \times (500 - 298)$$

$$\Delta H_2 - 37 = 18 \times 202$$

$$\Delta H_2 = 202 + 37$$

$$\Delta H_2 = 239 \text{ kJ}$$

$$= 23900 \text{ kJ}$$



$$(C_p)_A = 3$$

$$(C_p)_B = 5$$

$$(C_p)_C = 5$$

$$\Delta H_2 - \Delta H_1 = [3 \times 6 - 3 \times 1 - 5 \times 5] [500 - 298]$$

$$\Delta H_2 - 37000 = [18 - 28] \times 202$$

$$\Delta H_2 - 37000 = -2020$$

$$\Delta H_2 = 37000 - 2020$$

$$\Delta H_2 = 34980 \text{ J}$$

(Rxn Higher temp \rightarrow less Endothermic)

Q4,6

$$\Delta H_1 = -92.2 \text{ kJ}$$

$$\Delta H_2 = ?$$

$$T_2 = 373$$

$$T_1 = 298$$

$$\frac{106.7}{70.2} \\ \hline 36.5$$

$$\Delta H_2 - \Delta H_1 = (2 \times 35.1 - 3 \times 28.8 - 1 \times 29.1) (373 - 298)$$

$$\Delta H_2 + 92.2 = (70.2 - 77.6 - 29.1) (-75)$$

$$\Delta H_2 + 92.2 = (70.2 - 106.7) 75$$

$$\Delta H_2 + 92.2 = -45.3 \times 75$$

$$\Delta H_2 = -45.3 \times 75 - 92.2 \times 1000$$

~~$$\Delta H_2 = -45.3 \times 75 - 92.2 \times 1000$$~~

~~$$\Delta H_2 = -45.3 \times 75 - 92200$$~~

$$\Delta H_2 = -45.3 \times 75 - 92200$$

$$\Delta H_2 > \Delta H_1$$

more exothermic

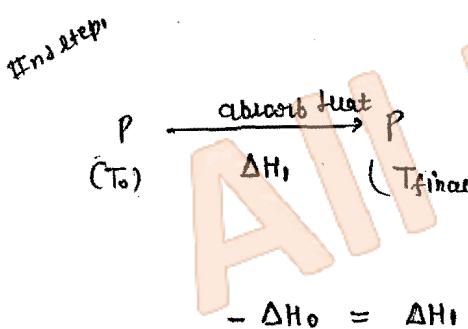
Adiabatic flame temp.

and

Adiabatic - Explosion temp.



(T_f)
complete
Combustion
 \downarrow
 $\text{CO}_2(g) + \text{H}_2\text{O}(l)$
(Only product)
(No Rxn)



1st step में उत्पादन तरेगा वह उत्पादक फ्रैम तम्प.

दूसरे करेगा वह तम्प जो 1st step में $-\Delta H_o$ दर्शाएगा

जिसका असर होता है तो यह complete combustion

अपरं अचल प्रकार तो adiabatic flame temp.

अपरं अचल वॉल्यूम तो adiabatic explosion temp.

$$-\Delta H_o = \sum n c_p \int_{T_0}^{T_f} dT$$

$$-\Delta H_o = \sum n c_p (T_f - T_0)$$

$$\frac{-\Delta H_o}{\sum n c_p} + T_0 = T_f$$

(product)

$$-\frac{\Delta E^\circ}{\Delta C_V} + T_0 = T_f$$

↓
at consti volume
(product)

Adiabatic flame temp.

⇒

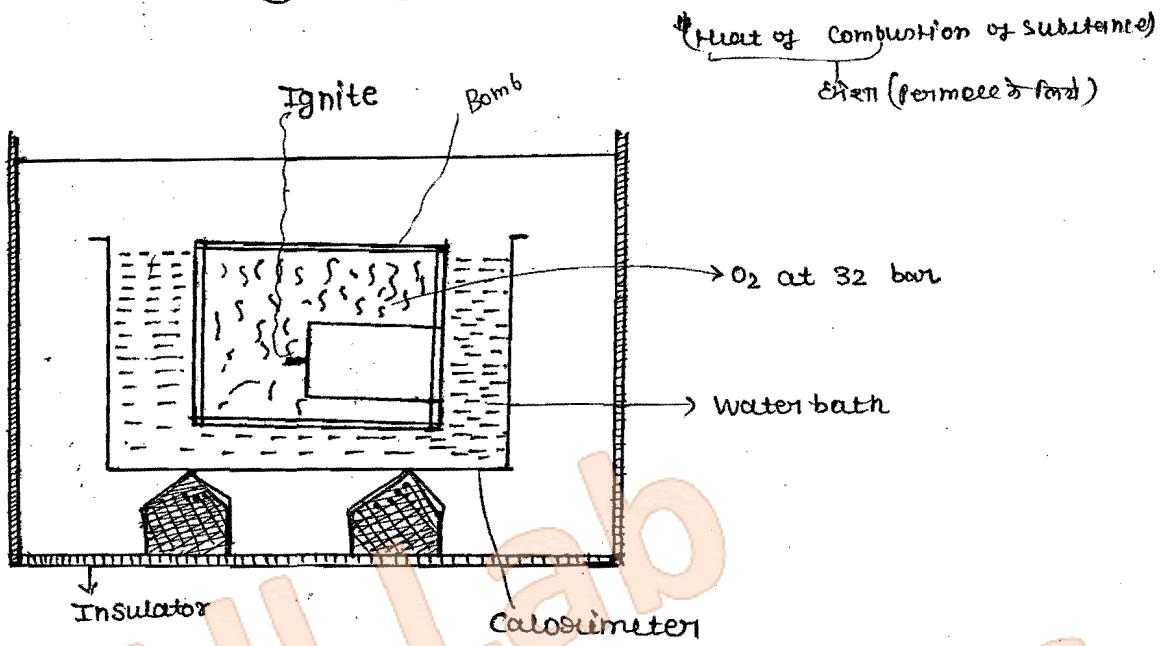
When a complete combustion of a substance take place, the final temp. which is achieved by product at consti-pressure condition is called A.F.T.

Adiabatic Explosion temp.

⇒ When a complete combustion of a substance take place the final temp. which is achieved by product at consti-volume condition is called A.E.T.

[\[Close\]](#)

BOMB - CALORIMETER



$$q_{\text{water}} = m C_{\text{water}} \Delta T$$

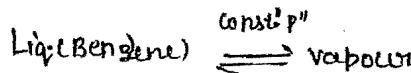
$$q_{\text{Bomb}} = m \times C_{\text{bomb}} \Delta T$$

$$q_{\text{combustion}} = q_{\text{water}} + q_{\text{Bomb}}$$

[17.11.15]

\Rightarrow Trouton's Rule: \Rightarrow [which under go condensation or dissociation] (failed)

$$\Delta S = \frac{\Delta H_{\text{vap.}}}{T_b}$$



\Rightarrow "For Molt of the liquid at a respective b.p.t.,
molar Entropy of vaporization ~~are~~ fixed.
which is 88 J K⁻¹ mol⁻¹ or 21 cal K⁻¹ mol⁻¹."

[Statement of Trouton's Rule]

88 J K⁻¹ mol⁻¹

or

21 cal K⁻¹ mol⁻¹

This law is failed which liquid is an oxidation or dissociation.

(like - CH₃COOH)

This law is also failed which having ^{very} High & very low b.p.t.

Gibbs- Helmholtz Equation:-

$$G = f(T, P, n_1, n_2, n_3, \dots, n_i)$$

$$\frac{dG}{dT} = \left(\frac{\partial G}{\partial T}\right)_{P, n_1, n_2, n_3, \dots, n_i} + \left(\frac{\partial G}{\partial P}\right)_{T, n_1, n_2, \dots} + \left(\frac{\partial G}{\partial n_1}\right)_{T, P, n_2} + \dots$$

at const - T, P

$$dG = dn_1 d\mu_1 + dn_2 d\mu_2 + dn_3 d\mu_3 + dn_4 d\mu_4 + \dots$$

Integrate both side

$$G_i = \mu_1 n_1 + \mu_2 n_2 + \mu_3 n_3 + \dots \quad \text{--- (2)}$$

Differentiate both sides

$$dG = n_1 d\mu_1 + \mu_1 dn_1 + dn_2 d\mu_2 + \mu_2 dn_2 + \dots \quad \text{--- (3)}$$

Subtract (3) - (2)

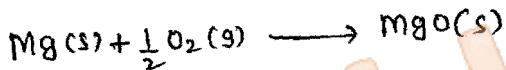
$$0 = n_1 d\mu_1 + n_2 d\mu_2 + n_3 d\mu_3 + n_4 d\mu_4 + \dots$$

$$\sum n_i \Delta H_i = 0$$



Gibb's Dheum Equation

TIFR Assignment



$$\Delta H_f^\circ = -602 \text{ kJ/mol}$$

$$\Delta S_f^\circ = -108 \text{ J/mol K}$$

$$\Delta G_f^\circ = \Delta H_f^\circ - T \Delta S_f^\circ$$

$$= -602 \text{ kJ/mol} - 273 \times (-108)$$

$$= -602 \text{ kJ/mol} + 29484 \text{ kJ/mol}$$

$$= 28882$$

$$\Delta G = \Delta H - T \Delta S$$

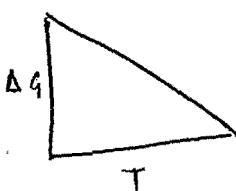
$$\gamma = nC + m\alpha$$

~~Qn. 3~~

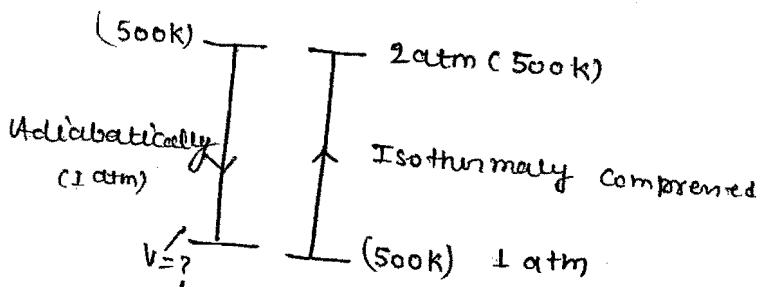
Slope { tan θ = $\frac{1}{\text{Base}}$ } = ~~3600 J CP~~

$$\frac{3600 \text{ J CP}}{40 \text{ C}}$$

$$\Rightarrow 75 \text{ J mol}^{-1} \text{ K}^{-1}$$



Qn. 20



[∴ ideal gas]

$$PV = nRT$$

$$\frac{P_1}{2 \times 1} = 1 \times 0.082 \times 500$$

$$V = \frac{0.082 \times 500}{2}$$

$$= 20.5 \text{ dm}^3$$

$$V_1 = 20.5 \text{ dm}^3$$

$$T_1 = 500 \text{ K}, T_2 = ?$$

$$\left(\frac{T_1}{T_2}\right)^{\gamma} = \left(\frac{P_2}{P_1}\right)^{1-\gamma}$$

$$\left(\frac{500}{T_2}\right)^{1.66} = \left(\frac{1}{2}\right)^{1-1.66}$$

$$\left(\frac{500}{T_2}\right)^{1.66} = \left(\frac{1}{2}\right)^{-0.66}$$

$$\left(\frac{500}{T_2}\right)^{1.66} = 1.58$$

$$\frac{500}{T_2} = (1.58)^{1/1.66}$$

$$\frac{500}{T_2} = 1.33$$

$$T_2 = \frac{500}{1.33} = 375.9$$

$$(P_1 V_1)^{\gamma} = \text{constant}$$

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

$$\left(\frac{V_1}{V_2}\right)^{\gamma} = \frac{P_2}{P_1}$$

$$\left(\frac{20.5}{V_2}\right)^{\gamma} = \frac{2}{1}$$

$$C_V = 1.5 R$$

$$\left(\frac{20.5}{V_2}\right)^{1.66} = 2$$

$$\frac{20.5}{V_2} = 1.5$$

$$C_P - C_V = R$$

$$C_P - 1.5R = R$$

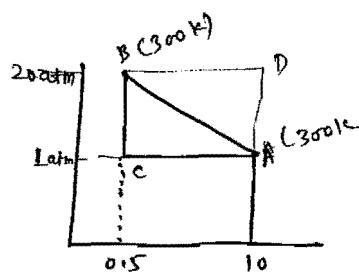
$$C_P = 2.5R$$

$$\frac{C_P}{C_V} = \gamma$$

$$\frac{2.5}{1.5} = \gamma$$

$$\gamma = \frac{5}{3} = 1.66$$

(27)



$$V_1 = 10 \text{ L}$$

$$V_2 = 0.5 \text{ L}$$

Expansion
isothermal (i.e. no work done)

$$W = -nRT \ln \frac{V_2}{V_1}$$

$$= -n \times 300 \times \ln \frac{0.5}{10}$$

$$= -\frac{10}{300} \times 300 \ln \frac{0.5}{100}$$

$$= -10 \ln \frac{5}{100} = (-) -10 \ln \frac{100}{5}$$

~~$= 10 \times (-)$~~ $= \underline{\underline{10 \ln 20}}$

$$PV = nRT$$

$$\frac{1 \times 10}{300} = nR$$

Q4.30

$$T_1 = 15^\circ\text{C}$$

$$T_2 = 75^\circ\text{C}$$

$$C_p \text{ of water} = 75 \text{ J K}^{-1} \text{ mol}^{-1}$$

$$\frac{\Delta H}{273} = nC_p$$

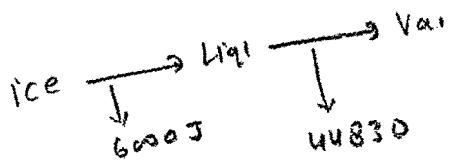
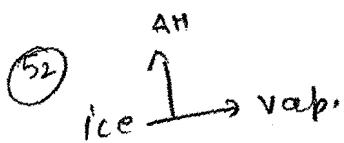
$$n = \frac{w}{m} = \frac{54}{18} = 3 \text{ mol}$$

$$\frac{\Delta H}{273} = 3 \times 75$$

$$\frac{\Delta H}{348-288} = 3 \times 75$$

$$\frac{\Delta H}{+60} = 3 \times 75$$

$$\Delta H = 13.5 \text{ kJ}$$



(53) $\ln \frac{P_2}{P_1} = \frac{\Delta H}{R} \left(\frac{T_2 - T_1}{T_1 T_2} \right)$

variation of temp. with pressure
 \rightarrow Celsius - Clapeyron Eqⁿ

$P_1 = 2.02 \times 10^3 \text{ N m}^{-2}$

$P_2 = 1 \text{ atm} = 1 \times 10^5 \text{ N m}^{-2}$

T_2
 1364

$\underline{\Delta H = 41 \text{ kJ mol}^{-1}}$

Leave yourself

$$\ln \frac{1 \times 10^5 \text{ Pa}}{2.02 \times 10^3} = \frac{41000}{81314} \left(\frac{T_2 - 293}{293 T_1} \right)$$

$$\ln \left(\frac{100}{2.02} \right) =$$

$$\ln 49.50 = 4931.44 \left(\frac{T_2 - 293}{293 T_1} \right)$$

~~$$3.982 = 4931.44 \left(\frac{T_2 - 293}{293 T_1} \right)$$~~

~~$$\frac{3.982 \times 293}{4931.44} = \left(\frac{T_2 - 293}{T_1} \right)$$~~

~~$$0.020 = 1 - \frac{293}{T_1}$$~~

~~$$1 - 0.020 = \frac{293}{T_1}$$~~

$$T_1 = \frac{293}{0.98}$$

- ? 201/10

Q4.57 $U = 3.5 PV + K$

$$V_1 = 0.25 \text{ m}^3$$

$$V_2 = 0.86 \text{ m}^3$$

$$P_1 = 5 \text{ Nm}^{-2}$$

$$PV^{1.3} = \text{constant}$$

where $\boxed{\gamma = 1.3}$

$$5 = \left(\frac{0.86}{0.25} \right)$$

Note →

(Water), $\Delta H_{\text{fusion}} = 324 \text{ kJ/kg}$ or 324 J/g

$$\Delta H_{\text{vapourization}} = 2264.76 \text{ kJ/kg}$$

$$c_p = \text{specific heat of water} = 4.18 \text{ J/g}$$

$$c_p = \text{specific heat of ice} = 2.023 \text{ J/g}$$

(Net γ previous)

$$\stackrel{Q_{1.2}}{\equiv} \Rightarrow PV^q = \text{constant}$$

$$T_1 V_1^{q-1} = T_2 V_2^{q-1} = k$$

$$\therefore T_2 > T_1$$

$\stackrel{Q_{1.28}}{=}$

$$q = -(q_{\text{water}} + q_{\text{cm}})$$

$$\frac{T_1 V_1^{q-1}}{V_2^{q-1}} = T_2$$

$$q_f = -2500 \times T \text{ kJ}^{-1} \times 4$$

$$\frac{T_1 V_1^{q-1}}{V_2^{q-1}} > T_1$$

$$q_f = -2500 \times (\Delta T)$$

$$\left(\frac{V_1}{V_2}\right)^{q-1} > 1$$

$$q_f = -2500 \times 4$$

$$q_f = -100 \text{ J}$$

$$\left(\frac{V_1}{V_2}\right)^{q-1} > \left(\frac{V_1}{V_2}\right)^0$$

$$q-1 < 0$$

$\alpha < 1$

$$n = \frac{6 \times 1}{500} = \frac{1}{100} = 0.01$$

$$q_{\text{combustion}}/\text{mole} = \frac{-10000 \text{ J}}{0.01}$$

$$= -100000 \text{ J}$$

$$q_{\text{combustion}} = -1000 \text{ kJ}$$

$$\stackrel{Q_{4.6}}{=} \frac{dP}{dT} = \frac{\Delta H}{T(V_{\text{vap.}} - V_2)}$$

Degrees of freedom

T_f , Rot, Vib

Linear



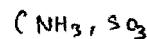
$$T_{lin} = 3$$

$$Rot_{lin} = 2$$

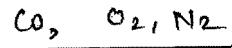
Non linear

$$T = 3$$

$$R = 3$$



$$(3N - 6)$$



$$T + R + V = 3N \quad (\text{No. of atom})$$

$$V = 3N - S$$

$$\begin{aligned} V &= 3 \times 2 - 5 \\ &= 6 - 5 \\ &= 1 \end{aligned}$$

(Contribution)



$$C_V \Rightarrow R/2$$

$$C_V \Rightarrow R \rightarrow R/2$$

$$C_V \Rightarrow V \rightarrow R \text{ at High}$$

$$0.5R \text{ at } T/2$$

0 at 0 W Temp.

$$(T) C_V = 3R/2$$

$$Rot_{lin} = 0$$

$$Vib_{lin} = 0$$

$$\text{Total } C_V = 3R/2 + 0 + 0$$

$$C_V = \frac{3R}{2}$$

$$\begin{aligned} CP &= C_V + R \\ CP &= \frac{5}{2}R \end{aligned}$$

$$\begin{cases} \frac{CP}{CV} = \frac{5}{3} = 1.66 \\ \downarrow \\ \text{(monatomic)} \end{cases}$$

The ratio of $\frac{C_p}{C_V}$ for diatomic gas O_2

Transl = 3

Rotat = 2

$$\begin{aligned}V &= 3N - 5 \Rightarrow \\&= 3 \times 2 - 5 \Rightarrow \\&= 1\end{aligned}$$

at High temp,

$$\begin{aligned}\text{Total } q_v &= 3 \times R/2 + 2 \times R/2 + 1 \times R \\&= 1.5R + R + R \\&= 3.5R \\&= \frac{7R}{2}\end{aligned}$$

$$C_p = C_v + R \Rightarrow \frac{7}{2}R + R = \frac{9R}{2}$$

$$\frac{C_p}{C_v} = \frac{9}{7} = 1.28$$

(29) $C_v = 20 \text{ J K}^{-1} \text{ mol}^{-1}$

Const. Volume, $T_2 = 2T_1$

$$\Delta E = q + w$$

w ≠ q

$$\Delta E = q + 0$$

$$C_v(T_2 - T_1) = q$$

$$20(2 \times 298 - 298) = q$$

$$q = 20 \times 298$$

$$q = 5960 \text{ J}$$

$$\boxed{q = 5960 \text{ J}}$$